Light amplification by seeded Kerr instability

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Amplification of femtosecond laser pulses typically requires a lasing medium or a nonlinear crystal. In either case, the chemical properties of the lasing medium or the momentum conservation in the nonlinear crystal constrain the frequency and the bandwidth of the amplified pulses. We demonstrate high gain amplification (greater than 1000) of widely tunable (0.5 to 2.2 micrometers) and short (less than 60 femtosecond) laser pulses, up to intensities of 1 terawatt per square centimeter, by seeding the modulation instability in an Y$_3$Al$_5$O$_12$ crystal pumped by femtosecond near-infrared pulses. Our method avoids constraints related to doping beam (disintegration of the spatial mode of an optical beam). The nonlinear Schrödinger equation with a Kerr third-order nonlinearity admits unstable solutions ($\theta$ $\neq$ 0) or the formation of oceanic ($\theta$ $\approx$ 0) and even multicycle pulses in the terahertz region ($\theta$ $\approx$ 0), where amplification schemes are presently nonexistent.

To characterize the gain, in the mathematical limit of continuous-wave seed and pump beams and infinitely extended in space, the amplification of mode-locked laser pulses typically proceeds through linear optical pumping of a gain medium followed by stimulated emission at lower photon energies than that of the pump. The medium stores the energy difference, and material damage limits the maximum amplified power. Recently, the quest for ever higher-average powers and broader wavelength tunability has resulted in the exploitation of optical parametric amplification ($\theta$ $\neq$ 0)—a second-order nonlinearity in which pump photons are split into pairs of conjugate lower-energy photons, without energy stored in the nonlinear crystal. However, phase matching and absorption of the pump and seed waves limits the center wavelength and the bandwidth of the amplified waves ($\theta$ $\approx$ 0). Improving phase matching and transparency requires intense development of new nonlinear crystals. We show that Kerr instability ($\theta$ $\approx$ 0), a third-order optical nonlinearity resulting in an intensity-dependent refractive index and common to any material, can compete with the more exploited parametric amplification.

The nonlinear Schrödinger equation with a Kerr third-order nonlinearity admits unstable solutions ($\theta$ $\neq$ 0), pumping a nonlinear medium with a sufficiently intense driver leads to weak waves that experience exponential gain as they propagate. When these weak waves are seeded from noise, the continuous wave breaks up into an unstable train of pulses ($\theta$ $\approx$ 0), leading to the disintegration of the spatial mode of an optical beam ($\theta$ $\approx$ 0) or the formation of oceanic ($\theta$ $\approx$ 0) and optical rogue waves ($\theta$ $\approx$ 0). Despite the wide occurrence of Kerr instabilities in physics, the theoretical understanding is still limited to instabilities at frequencies comparable with that of the pump ($\theta$ $\approx$ 0). Recently, a fully analytical theory of Kerr instabilities valid for perturbations of arbitrary frequencies has been developed ($\theta$ $\approx$ 0) that predicts appreciable gain over a broad spectral range between about zero and twice the pump frequency. Here, we experimentally demonstrate seeded amplification of femtosecond laser pulses in the visible and infrared spectral regions. By seeding gain at different wavelengths, it is possible to amplify femtosecond laser pulses over more than an octave bandwidth (Fig. 1). A comparison is shown for seed spectra at three different central wavelengths (0.6, 1.4, and 1.8 $\mu$m) (Fig. 1, pale colored solid lines) with the corresponding amplified spectra (Fig. 1, bright colors, solid lines). The gain medium is a Y$_3$Al$_5$O$_12$ (YAG) crystal pumped by long femtosecond pulses from a Ti:sapphire laser. Gain in excess of 1000 is achieved throughout the whole bandwidth spanning 0.5 to 2.2 $\mu$m by simply adjusting the angle $\theta$ (Fig. 1) between the seed and the pump beams. Not only can the gain be tuned to the desired wavelength, but the spectral bandwidth is also larger. At 1.4 $\mu$m, for example, the 100-nm bandwidth of the seed is fully amplified. Despite the strong nonlinearity and the complex propagation of the pump through the crystal, the seed pulses propagate and amplify without appreciable phase modulation. We measured the amplified pulses with second-harmonic frequency resolved optical gating (SH-FROG). As demonstrated in Fig. 1, insets A to D, the duration of the amplified pulses remains close to the transform limit of the seed, in any case <60 fs, and can even be shorter than the seed by pumping with short pulses (fig. S1). Furthermore, the beam quality is preserved during amplification (fig. S1). Our newly developed theory suggests that single-cycle pulses can potentially be amplified by controlling the pump and seed wavelengths. Therefore, together with automatic phase matching demonstrated below, Kerr amplification offers an interesting new approach to amplifying single-cycle pulses in the visible ($\theta$ $\approx$ 0), infrared (14–16), and even multicycle pulses in the terahertz region (17), where amplification schemes are presently nonexistent.

To characterize the gain, in the mathematical limit of continuous-wave seed and pump beams and infinitely extended in space, the amplification.

Fig. 1. Amplified spectra and pulse durations. Experimental amplified spectra (bright colors) and seed spectra (pale colors) for amplification around 0.5 $\mu$m (green), 1.4 $\mu$m (yellow), and 1.8 $\mu$m (blue), normalized to corresponding amplified spectra. The pump spectrum at 0.8 $\mu$m is shown in red. The angle between the pump and the seed laser beams ($\theta$) is reported close to each amplification spectra. The pulse durations measured with a SHG-FROG are plotted in the insets for amplification spectra centered at (A) 1.4 $\mu$m, (B) 1.75 $\mu$m, and (C) 1.95 $\mu$m, and (D) for the seed at 1.8 $\mu$m. The amplified pulses at 1.4 $\mu$m preserve the seed pulse duration of 45 fs [inset (A)]. Although the 1.8-$\mu$m seed pulses last only 15 fs (close to transform limit), the angular chirp of the amplification process narrows the spectrum that enters the FROG apparatus, which is positioned a few meters away from the YAG crystal. The measured spectra associated with insets (B) and (C) are plotted with purple lines. Each slice of the spectrum generates transform limited pulses (at 1.75 $\mu$m the measured bandwidth is 76 nm, and at 1.85 $\mu$m it is 100 nm).
Fig. 2. Dependence of gain on pump and seed powers. (A) The amplification factor (the ratio between amplified and seed powers, spectrally integrated) increases exponentially with pump pulse energy, in agreement with theoretical expectation (black dotted line), which is reported in the supplementary materials (18), but saturates for pump energies higher than 150 μJ, which are close to the damage threshold of YAG (~300 μJ, corresponding to a vacuum intensity of 10 TW/cm²). (B) As a function of seed pulse energy, amplification remains high (>1000) for seed energies <0.2 nJ but decreases with a polynomial behavior for higher seed energies. Seed energy is varied at the maximum pump power (purple circles), whereas pump energy is varied at the seed energy just before the onset of saturation (yellow circle). The seed center wavelength is 1.4 μm.

Fig. 3. Angular chirp of the amplified spectrum. Amplified spectrum centered around 1.8 μm as a function of propagation angle, measured in the far field. The angular chirp of 3 μm/rad and the emission angle agree with the theoretical prediction (gray dashed line). It is the angularly integrated spectrum that is plotted as a blue line in Fig. 1.

proceeds exponentially with the length of the crystal with intensity gain coefficient (7)

\[
g(\Omega) = \frac{k_p(\omega_p)k_n(\omega)}{\sqrt{k_p^2(\omega) - (\alpha D_u)^2}}
\]

Here, \(\Omega = \omega - \omega_0\) is the frequency shift between seed (\(\omega_0\)) and pump (\(\omega_p\)), \(k(\omega) = (\omega_0 + i \Omega) \sqrt{n_r^2 I_p/c}\) is the nonlinear wavevector, and \(I_p\) and \(n_r\) are the pump intensity and the nonlinear refractive index, respectively. \(k_p^2(\omega_p)\) is the total wavevector of the pump given by adding the linear wave vector \(k = \omega_0 n(\omega)/c\) to the nonlinear wave vector at the pump wavelength, \(\sigma = (k_n + D_{2u}/\omega)\), where \(k_n^2(\omega) = k_p^2(\omega) + 2k_p^2(\omega)\) is the seed wave vector (the nonlinearity is added twice compared with \(k_p\)). \(D_{2u}\) takes into account the dispersion of the medium to any frequency shift (7). Amplification of finite pulses and Gaussian beams modifies this ideal gain factor by taking into account the temporal and spatial geometry (supplementary materials (18)).

We measured exponential growth with respect to pump intensity (Fig. 2A), in agreement with the theoretical prediction (Fig. 2A, dashed black line), up to saturation of the gain, which occurs close to the damage threshold of YAG. As a function of seed pulse energy (Fig. 2B), the gain remains constant up to 0.2 nJ and then also saturates. Saturation limits the amplified intensity to 1 TW/cm², which is ~10% of the pump intensity (the seed pulses are shorter than the pump, and the seed beam waist at the focus is smaller) (supplementary materials (18)). Near saturation, we observed cross-talk between the two similarly intense beams in the reduction of the speckle pattern generated by the pump beam. The maximum amplified energy is 1.6 μJ (from 40-nJ seed and 270-μJ pump), corresponding to an energy conversion efficiency of 0.6%. Chirped pulse amplification (19, 20) can be used to increase the output energy.

We next demonstrated that phase matching still plays a role in Kerr amplification, as it does everywhere in nonlinear optics, by forcing different frequencies to propagate at slightly different directions, with angle \(\theta = \sin^{-1}(\sqrt{\bar{n}(k_p + \alpha D_u)})\) with respect to the pump beam. Here, \(\bar{n}(k_p) = (k_p^2 - D_{2u}^2)/(\sigma^2 - 1)\) is the transverse momentum that experiences maximum gain. In contrast to conventional three- or four-wave mixing processes, however, here phase matching is automatically satisfied (7). The measured angular chirp (Fig. 3) matches the theoretical prediction well. Because the chirp is almost linear with wavelength, it will be possible to compensate for the beam divergence that phase matching imposes with a dispersive element placed just after the medium. Furthermore, the angular chirp is only weakly dependent on the pump intensity (fig. S6), suggesting that it is uniform across the amplified beam profile. Matching the transverse momentum of optimum gain is a critical parameter to achieve amplification. Optimum amplification of a desired wavelength is achieved in the experiment by tuning the angle \(\theta\) (Fig. 1). And as confirmed in Fig. 3, the measured optimum angle coincides with that predicted by theory.

By using near-infrared pump pulses, we have demonstrated seeded amplification by means of Kerr instability of short femtosecond pulses over a wide tunable spectral range. Amplification occurred in a crystal (YAG) whose nonlinear refractive index is of average magnitude. The nonlinearity is at least 100 times stronger in special materials such as chalcogenide glasses (21) or graphene (22) or at frequencies at which the linear permittivity approaches zero (23). In the latter case, a total index change of 170% has been observed. Therefore, high gain amplification seems feasible in only a few micrometers, if not nanometers, of these materials, with gain coefficients as high as \(g \sim 100 \text{ s mm}^{-1}\) (as opposed to \(\sim 5 \text{ mm}^{-1}\), as in YAG).

Our theory predicts that gain terminates at frequencies for which either \(\chi^2 < 0\) or \(k_p^2 = (\alpha D_u)^2\). In KBr pumped by 2.1-μm femtosecond pulses, the cut-off extends to 14 μm (~21 THz), and to 42 μm (~7.1 THz) in the CW limit, therefore up to far-infrared frequencies, at which nonlinear crystals perform poorly or amplification schemes are inexcetable altogether. Neither linear gain media nor \(\chi^2\) nonlinear crystals offer as wide a bandwidth tunability because of limitations in achieving phase matching (4) or because of narrow gain profiles. Several nonlinear crystals also absorb mid-infrared light (24).

The energy output can be scaled up to arbitrarily high energies by adapting chirped pulse amplification schemes (19, 20). Furthermore, the amplified bandwidth can sustain single-cycle pulses. Therefore, Kerr amplification will result in a shift of design paradigm for next-generation high-intensity laser sources. For the moment, the demonstrated microjoule-level pulse energies are already suitable to trigger strong-field processes in condensed matter—such as high harmonic generation (25), ablation and damage (26), optically driven currents (27), and photoemission (28)—and to study highly excited Rydberg states (29).

Given the broad occurrence of Kerr nonlinear instabilities in nature (10, 11), our demonstration with femtosecond laser pulses may prove useful to address the spatiotemporal evolution of instabilities in forms other than light over a broad range of frequencies, where the effect of the full linear and nonlinear (23) dispersion of the medium becomes important.
REFERENCES AND NOTES

18. Materials and methods are available as supplementary materials.
19. B. Schmidt for insightful discussions. All data needed to evaluate the conclusions in the paper are present in the paper and/or the supplementary materials.

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SUPPLEMENTARY MATERIALS

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Materials and Methods
Supplementary Text
Figs. S1 to S6
References (30–34)

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Seeding a laser amplifier
Amplification of femtosecond laser pulses requires a lasing medium or a nonlinear crystal. The chemical properties of the lasing medium or adherence to momentum conservation rules in the nonlinear crystal constrain the frequency and the bandwidth of the amplified pulses. Vampa et al. seeded modulation instability in a laser crystal pumped with femtosecond near-infrared pulses. This provided a method for the high gain amplification of broadband and short laser pulses up to intensities of 1 terawatt per square centimeter. The method avoids constraints related to doping and phase matching and can be expected to be applied to a wide pool of glasses and crystals.
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Supplementary Material for

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This PDF file includes:

Materials and Methods
Supplementary Text
Figs. S1 to S6
References
Materials and Methods

Femtosecond laser pulses centered around 0.8 µm (the “pump”) are loosely focused (≈ f/200) in a 2 mm thick YAG crystal to a peak intensity in vacuum between 3 and 9 TW/cm². The seed beam is more strongly focused (≈ f/10 – f/30) than the pump. At these intensities, the pump beam becomes unstable during propagation in the crystal and a visible speckle pattern is observed at the output as the combined result of self-phase modulation and spatial modulation instability.

Two separate experiments have been conducted.

In the first experiment, a Ti:Sapphire laser delivering ~ 1 mJ, 30 fs pulses at 1kHz repetition rate has been used to amplify 0.5 µm and 1.4 µm pulses. A broadband seed spanning from 0.5 µm to 1.6 µm is obtained by self-phase modulation in a 3 mm thick sapphire plate with a small fraction of the pump energy. Amplification of 0.5 µm pulses proceeds directly from this super-continuum. The seed at 1.4 µm is obtained by parametric amplification of the infrared portion of the super-continuum with a fraction of the pump in a 3 mm thick type-II BBO crystal. Clean pulses of 45 fs duration are generated. Seeds at 0.5 µm and 1.4 µm are then focused (f/30) into a 2 mm YAG crystal, where they overlap in space and time with the 0.8 µm pump, whose beam size and power are controlled to optimize gain. The pump pulses used for the amplification have been stretched to 140 fs to avoid inducing phase modulation on the seed.

In the second experiment, a Ti:Sapphire laser delivering 16 mJ, 50 fs pulses at 100 Hz repetition rate has been used to amplify the broadband spectrum around 1.8 µm. The broadband seed at 1.8 µm is obtained by spectral broadening in a 1 m long hollow-core fiber of 1.3 mJ pulses obtained from a commercial Optical Parametric Amplifier (Light Conversion, HE-TOPAS-C) pumped by 7 mJ of 0.8 µm pulses. The broadband seed can be compressed down to 15 fs (2.5 optical cycles), as measured with a dispersion-free SHG FROG. The seed is then focused (f/10) into the same YAG crystal of the first experiment, together with a fresh pump (whose beam size and power are controlled like in the first experiment). Again, the pump pulses have been stretched to 140 fs.

We have also achieved amplification in Fused Silica but with lower gain, due to the lower n₂ and damage thresholds compared to YAG. This data is not presented here.

Supplementary Text

Calculation of gain

The scaling of the amplification factor with the intensity of the pump (black dashed line in Fig. 2A) is calculated as:

\[ \frac{W_s(l)}{W_s(0)} = \frac{w_x}{\sqrt{Re[q_x]}} e^{\int g(z) dz} \quad (S1), \]

where \( W_s(z) \) is the seed power, \( w_x \) is the seed beam width, \( q_x = w_x^2 + 2(g_2 + i\alpha)l \), \( g(z) \) is the gain coefficient calculated with Eq. 1, and \( \alpha(\Omega) = \sigma D_u/[k_p^2 - (\sigma D_u)^2] \). Because of the non-collinear geometry between seed and pump, the seed experiences inhomogeneous gain along its propagation direction “z”. The inhomogeneous gain is encoded by varying the pump intensity \( I_p \) as a function of \( z \):
\[ I_p(z) = I_p \exp\left[\frac{-2z^2}{w_{p,eff}^2}\right], \]

where \( I_p \) is the peak intensity in the middle of the pump beam. The integral runs over the overlap region between seed and pump. \( g_2 \) represents the width of the gain profile in momentum space. Both \( g_2 \) and \( \alpha \) are defined in Ref. (7).

The length of the interaction ‘\( l \)’ is estimated by considering the propagation angle between the seed and the pump and the size of both beams. The propagation angle in air is 14°. This is reduced to 8.1° upon refraction of the pump at the entrance surface of YAG. The waist diameter of the seed (1/e²) is \( w_x = 54 \mu m \), the pump waist diameter is 226 μm, so the two beams overlap for \( l = 1.6 \text{ mm} \), and the effective width of the pump beam seen by the seed is \( w_{p,eff}^2 = 880 \mu m \).

Equation S1 is equivalent to Eq. (21) of Ref. (7), in the limit where only the geometric properties of the amplification are retained. That is, we set \( \tau = \tau_g(l), \Gamma_s' = 0, \vec{k}_e = \vec{k}_{s,e} \). Technically, we equate the input and output pulse durations (in agreement with the experimental results at 1.4 µm), neglect dispersion of the gain coefficient, and we set the angle between seed and pump to optimize amplification of the seed center wavelength (like in the experiment). Compared to Ref. (7), we introduce the integral over the distance in the exponent, but neglect it in the prefactor. We find that, although the momentum overlap between gain and seed beam changes with distance – and would be encoded in a \( z \)-dependent \( q_x(z) \) – the prefactor contributes little to the general exponential trend. Much more important is taking proper account of the \( z \)-dependent gain, which almost halves the gain coefficient (and therefore the slope of the black dotted line in Fig. 2A) compared to the CW case of Eq. 1.

Other parameters required to plot the theoretical scaling are pump wavelength \( \lambda_p = 0.8 \mu m \), seed wavelength \( \lambda_s = 1.4 \mu m \), nonlinear index of YAG \( n_2 = 6.2 \times 10^{-16} \text{ cm}^2/\text{W} \) (30). The linear refractive index of YAG is taken from Ref. (31). The Sellmeier expansion is:

\[
n^2 - 1 = \frac{2.282\lambda^2}{\lambda^2 - 0.01185} + \frac{3.27644\lambda^2}{\lambda^2 - 282.734}.
\]

The group velocity at the pump wavelength (800 nm) is \( +97 \text{ fs}^2/\text{mm} \). The intensities in Fig. 2 range from 3 – 9 TW/cm².

**Spatial profile of amplified beam**

Despite the exponential dependence of the amplified pulse energy on the pump, and the strong spatial modulation on the pump, the amplified beam is rather clean. To demonstrate this, the beam at 1.4 µm has been frequency doubled in a BBO crystal and the focus of the second harmonic imaged (Fig. S1). Without the BBO, or when either the seed or the pump is blocked, the beam disappears, indicating that it is the amplified 1.4 µm that is being frequency doubled.

**Bandwidth of the amplified pulses**
The spectral bandwidth of the amplified pulses is largely determined by how well the transverse momentum of each wavelength in the seed spectrum overlaps with the gain bandwidth for that wavelength. The maximum of the latter shifts with wavelength and results in angular chirp of the amplified spectrum. Therefore, one way to increase the amplified spectral bandwidth is to propagate each wavelength at the optimum angle with respect to the pump beam. A similar approach has been employed in $\chi^{(2)}$ amplification, and is referred to as “achromatic phase matching” (32).

Alternatively, one could increase the width of the momentum distribution of the seed beam by focusing the beam more strongly. This is demonstrated in Fig. S2, where the amplified bandwidth around 0.5 µm is increased from 20 nm with $f = 30$ cm to 30 nm with $f = 15$ cm. The drawback is that the intensity in the seed beam also increases, which may result in earlier saturation of the amplification process and lower amplified pulse energy.

Broad amplified bandwidths can even be generated directly during amplification by pumping with short pump pulses and narrow-band seed pulses. The instantaneous nature of the $\chi^{(3)}$ response of YAG assures that amplification takes place only when the pump is present. To demonstrate this effect, a 10 nm bandwidth-limited seed around 0.5 µm is amplified to 16 nm bandwidth pulses, consistent with the 30 fs duration of the pump (see Fig. S3). Near-infrared pulses of < 5 fs duration are routinely achieved in attosecond laboratories (12). They can be used to generate and amplify few-cycle pulses at mid-infrared wavelengths from near-CW seed beams, thereby overcoming the challenging task (4) of directly amplifying octave-spanning bandwidths with second-order nonlinearities (33, 34). In the limiting case, truly CW lasers can potentially be pulsed as well.

Too much power distorts the amplified pulses

Figure S4 shows the spectrum of the amplified pulses for increasing seed pulse energy. When the seed energy is above 40 nJ, the amplified spectrum is broadened significantly (red line in panel A), most likely from cross-phase modulation with the pump. The amplified energy of 1.6 µJ corresponds to an intensity of 3.5 TW/cm². Moreover, it seems that the spectral phase acquires a higher third-order contribution (dashed lines in panel B), which renders the pulse more asymmetric (panel C). Cross-talk between the two similarly intense beams is observed in the suppression of the visible speckle pattern generated by the pump beam. Due to the exponential sensitivity of the amplification process on the pump intensity, we speculate that depletion of the pump beam along the interaction length quenches amplification.

Dependence of angle of optimum gain on pump wavelength

As discussed in the text, optimum amplification occurs only if the lateral momentum of the seed coincides with the lateral momentum of maximum gain, $k_\perp$. The angle that the maximally amplified seed forms with the pump, which coincides with the emission angle in our experiment (dashed gray line in Fig. 3), can be calculated with $\sin \theta =$
\( \kappa_L / (k_p + \sigma D_u) \). The variation of this angle with wavelength of the seed represents the angular chirp of the amplified beam. Like \( \kappa_L \), the chirp depends on the frequency shift \( \Omega \) between the seed and pump wavelengths. Figure S5 shows how the chirp in the infrared to mid-infrared spectral regions is halved by pumping at 1.03 \( \mu \)m, rather than at 0.8 \( \mu \)m.

Furthermore, Fig. S6 show that the theoretical angular chirp varies only weakly with the pump intensity. Here, the difference in the higher and lower intensities corresponds to a drop of the amplification factor by 99\%. Therefore, our calculation suggests that the angular chirp is uniform across the amplified beam profile – a necessary condition for its compensation with simple optical elements.
Fig. S1.

Amplified beam quality. Image of the second harmonic of the amplified beam at 1.4 µm, taken at the focus. The image indicates that the beam quality of the seed is preserved during amplification.
**Fig. S2.**

**Seed focusing controls the amplified bandwidth.** The amplified bandwidth increases from 20 nm to 30 nm when the seed focus length decreases from 30 cm to 15 cm.
Fig. S3.

**Short pump pulses increase the amplified bandwidth.** When the pump pulses (of 30 fs duration) are shorter than the seed pulses (green line, transform limit of 42 fs), the amplified spectrum (blue line) is broadened to sustain pulses as short as the pump (transform limit of 26 fs).
Fig. S4.

**High seed energy broadens the amplified spectrum.** The amplified spectrum is excessively broadened for seed pulse energies above 40 nJ (red trace in panel A). The broadening is associated with increased third-order spectral phase (red dashed line in panel B) with respect to lower seeding pulse energy (dashed green line in panel B). In the temporal domain (panel C), the amplified pulse becomes slightly asymmetric (red line compared to green line). The spectral amplitude and phase and the pulse duration have been reconstructed with a dispersion-free SHG FROG.
Fig. S5.
**Dependence of emission angle with pump wavelength.** The emission angle (inside the crystal) in the infrared and mid-infrared spectral region can be halved by pumping at 1.03 µm (red line) rather than at 0.8 µm (black line).
Fig. S6.  
**Dependence of the angular chirp on pump intensity.** The angular chirp varies weakly by decreasing the pump intensity. The calculated chirp is for pump center wavelength at 0.8 µm, and for a YAG crystal (the parameters are given in the supplementary text). The highest pump intensity (9 TW/cm²) corresponds to a pump energy of 270 µJ.
References and Notes


18. Materials and methods are available as supplementary materials.


